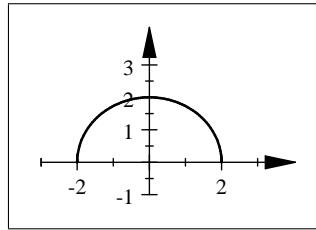


## 1.1 Domain and range of some functions

Function	Domain	Range
$\sqrt{a^2 - x^2}$	$[-a, a]$	$[0, a]$
$\sqrt{x^2 - a^2}$	$(-\infty, -a] \cup [a, \infty)$	$[0, \infty)$
$\sqrt{x^2 + a^2}$	$\mathbb{R}$	$[a, \infty)$

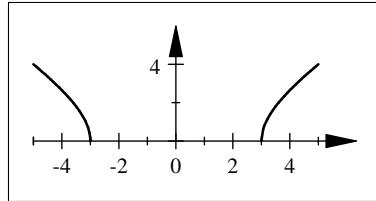
Exp (1)  $f(x) = \sqrt{4 - x^2}$  (see Ex. 38 in 1.1 )  
 $f(x) = \sqrt{4 - x^2}$



$D = [-2, 2]$  , Range  $= [0, 2]$

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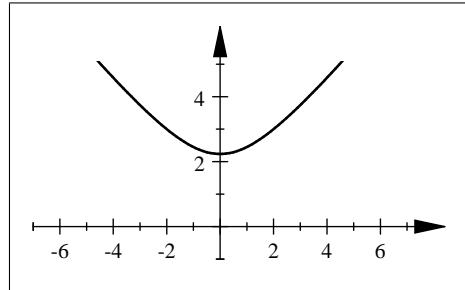
Exp (2)  $f(x) = \sqrt{x^2 - 9}$



$D = (-\infty, -3] \cup [3, \infty)$  , Range  $= [0, \infty]$

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Exp (3)  $f(x) = \sqrt{x^2 + 5}$



$$D = \mathbb{R} , \text{ Range} = [\sqrt{5}, \infty)$$


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### 1.3

Add exc. 30

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### 2.2

$$\lim_{x \rightarrow a} \frac{1}{(x-a)^n} = \begin{cases} \infty & n \text{ even} \\ n & \text{odd} \end{cases} \quad \begin{cases} \lim_{x \rightarrow a^+} \frac{1}{(x-a)^n} & \infty \\ \lim_{x \rightarrow a^-} \frac{1}{(x-a)^n} & -\infty \end{cases}$$


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2.5 Delete exp.(4)

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### 2.6

$$\lim_{x \rightarrow \pm\infty} (a_n x^n + a_{n-1} x^{n-1} + a_{n-2} x^{n-2} + \dots + a_2 x^2 + a_1 x + a_0) = \lim_{x \rightarrow \pm\infty} (a_n x^n)$$


---

$$\lim_{x \rightarrow \pm\infty} x^n = \begin{cases} \infty & n \text{ even} \\ n & \text{odd} \end{cases} \quad \begin{cases} \lim_{x \rightarrow +\infty} x^n & \infty \\ \lim_{x \rightarrow -\infty} x^n & -\infty \end{cases}$$


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### 3.3

After exp.(5)

$$\begin{aligned} \text{(i)} \quad & \lim_{x \rightarrow 0} \frac{\sin nx}{mx} = \frac{n}{m} \\ \text{(ii)} \quad & \lim_{x \rightarrow 0} \frac{\sin nx}{\tan nx} = \frac{n}{n} \\ \text{(iii)} \quad & \lim_{x \rightarrow 0} \frac{\tan nx}{mx} = \frac{n}{m} \\ \text{(iv)} \quad & \lim_{x \rightarrow 0} \frac{mx}{\tan nx} = \frac{m}{n} \end{aligned}$$

After exc.(41)

$$\begin{aligned} \text{(i)} \quad & \lim_{x \rightarrow 0} \frac{\tan nx}{\sin mx} = \frac{n}{m} \\ \text{(ii)} \quad & \lim_{x \rightarrow 0} \frac{\sin mx}{\tan nx} = \frac{m}{n} \end{aligned}$$